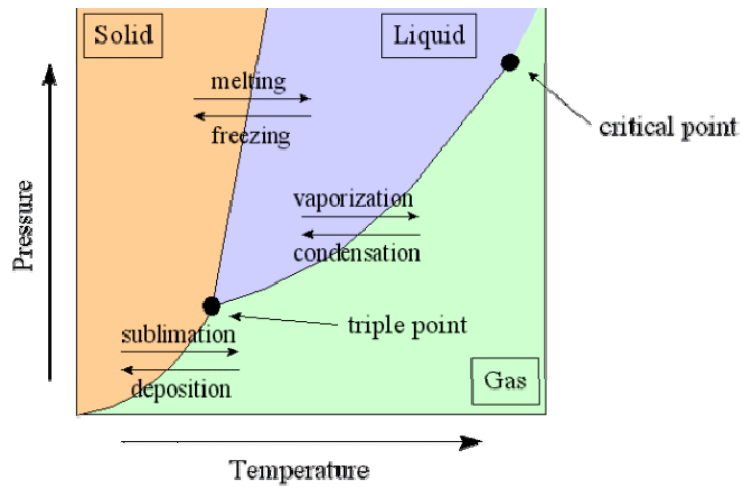


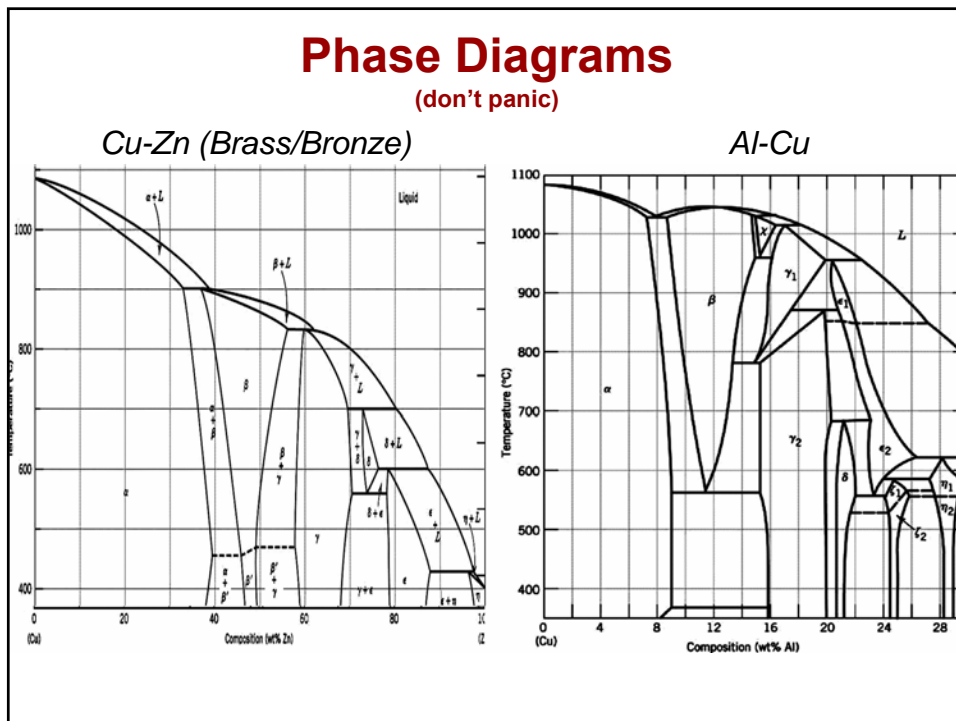
# Phase Diagrams

Multiple variables can be plotted:  
**Chemists are used to Pressure vs. Temperature.**  
**Metallurgists: Temperature vs. Binary Composition,**  
**Nobody: Pressure vs. Binary Composition**



# Phase Diagrams

(don't panic)

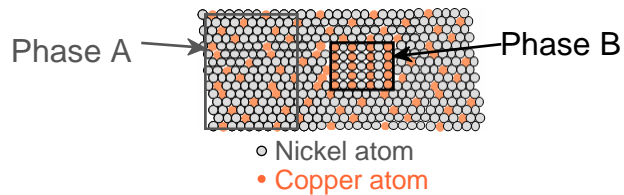


## Phase Diagrams

nice tutorial: <http://www.soton.ac.uk/~pasr1/>

### ISSUES TO ADDRESS...

- When we combine two elements...  
what **equilibrium** state do we get?
- In particular, if we specify...  
a composition (e.g., wt% Cu - wt% Ni), and  
a temperature ( $T$ )  
then...  
How many phases do we get?  
What is the composition of each phase?  
How much of each phase do we get?



## Phase Diagrams

For a phase diagram with temperature on the vertical axis,  
a **solidus** is a line below which the substance is  
**stable in the solid state.**

A **liquidus** is a line above which the substance is  
**stable in a liquid state.**

**There may be a gap between the solidus and liquidus;  
within the gap, the substance is in equilibrium only  
with solid and liquid both present.**

The **triple point** of a substance is the temperature and pressure  
at which three phases (gas, liquid, and solid)  
of that substance can coexist.

## Solid Solutions

A **solid solution** is a solid-state solution of one or more solutes in a solvent.

Solid Solution and **not** a compound **IFF** crystal structure of remains unchanged by addition of the solutes **and** the mixture remains in a single homogeneous phase.

Solute incorporation either *substitutionally or interstitially*

**Solid solutions may form if the solute and solvent have:**

- Similar atomic radii (15% or less difference)
- Same crystal structure
- Similar electronegativities
- Similar coordination number (a.k.a. valency)

## Eutectics

**eutectic:** the composition of a mixture that has the lowest melting point where the phases simultaneously crystallize from molten solution at this temperature.

From the Greek 'eutektos', meaning 'easily melted'.

When a non-eutectic alloy freezes, one component of the alloy crystallizes at one T and the other at a different T.

With a eutectic alloy, the **mixture freezes as one at a single T.**

A eutectic alloy therefore has a sharp melting point, and a non-eutectic alloy exhibits a plastic melting range.

## Uses of Eutectic Phases

soldering: Sn and Pb and sometimes Ag or Au.

casting alloys: Al-Si, cast iron (austenite-cementite Fe-C)

brazing: diffusion removes alloying elements from the joint.

temp. response: Wood's (Bi-Pb-Sn-Cd, mp 70 C) &  
Field's (Bi-In-Sn, mp 62 C) metals  
for fire sprinklers, prototype casting, repairs

non-toxic mercury replacements: galinstan (Ga-In-Sn)

NaK alloys: liquid at room temperature, used as coolant in  
fast neutron nuclear reactors.

## Phase Equilibria: Solubility Limit

### Introduction

- Solutions – solid solutions, single phase
- Mixtures – more than one phase

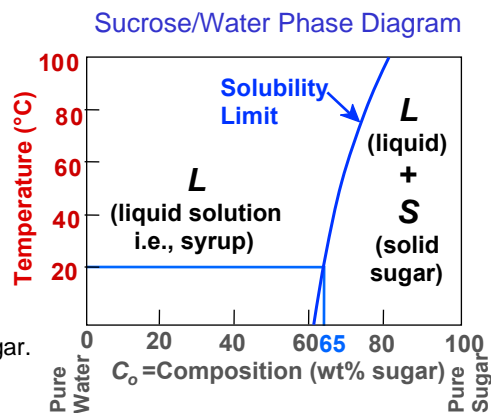
- **Solubility Limit:**  
Max concentration for  
which only a single phase  
solution occurs.

Question: What is the  
solubility limit at 20°C?

Answer: 65 wt% sugar.

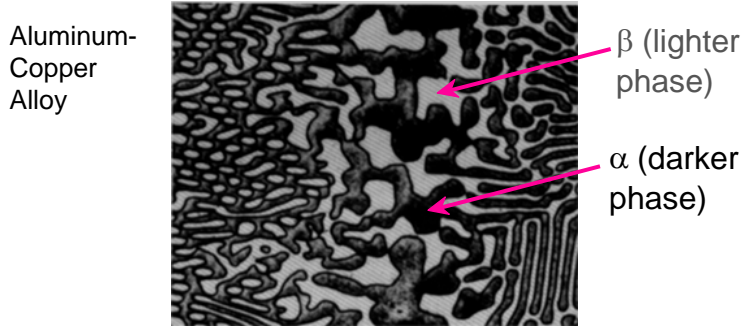
If  $C_O < 65$  wt% sugar: syrup

If  $C_O > 65$  wt% sugar: syrup + sugar.



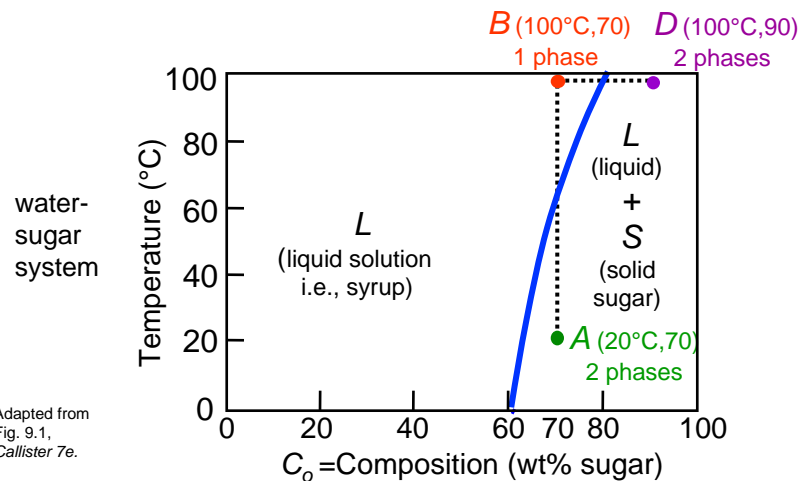
## Components and Phases

- **Components:**  
The elements or compounds which are present in the mixture (e.g., Al and Cu)
- **Phases:**  
The physically and chemically distinct material regions that result (e.g.,  $\alpha$  and  $\beta$ ).



## Effect of $T$ & Composition ( $C_o$ )

- Changing  $T$  can change # of phases: path  $A$  to  $B$ .
- Changing  $C_o$  can change # of phases: path  $B$  to  $D$ .



## Phase Equilibria

Simple solution system (e.g., Ni-Cu solution)

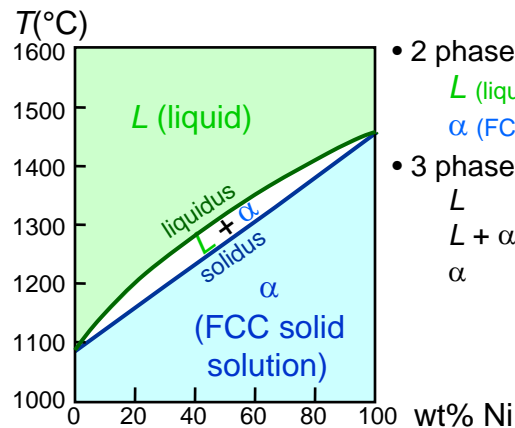
	Crystal Structure	electroneg	$r$ (nm)
Ni	FCC	1.9	0.1246
Cu	FCC	1.8	0.1278

- Both have the same crystal structure (FCC) and have similar electronegativities and atomic radii (W. Hume – Rothery rules) suggesting high mutual solubility.
- Ni and Cu are totally miscible in all proportions.

## Phase Diagrams

- Indicate phases as function of  $T$ ,  $C_0$ , and  $P$ .
- For this course:
  - binary systems: just 2 components.
  - independent variables:  $T$  and  $C_0$  ( $P = 1$  atm is almost always used).

• Phase Diagram for Cu-Ni system



- 2 phases:
  - $L$  (liquid)
  - $\alpha$  (FCC solid solution)
- 3 phase fields:
  - $L$
  - $L + \alpha$
  - $\alpha$

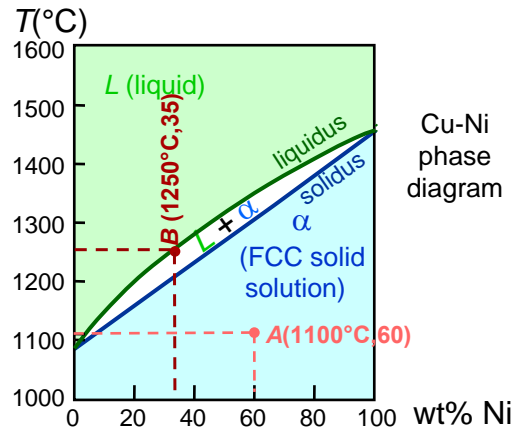
## Phase Diagrams: # and types of phases

- Rule 1: If we know  $T$  and  $C_o$ , then we know the # and types of phases present.

- Examples:

$A(1100^\circ\text{C}, 60)$ :  
1 phase:  $\alpha$

$B(1250^\circ\text{C}, 35)$ :  
2 phases:  $L + \alpha$



## Phase Diagrams: composition of phases

- Rule 2: If we know  $T$  and  $C_o$ , then we know the composition of each phase.

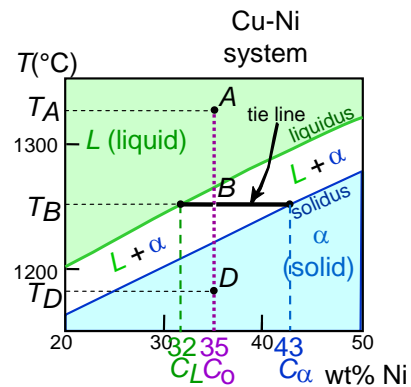
- Examples:

$C_o = 35 \text{ wt\% Ni}$

At  $T_A = 1320^\circ\text{C}$ :  
Only Liquid ( $L$ )  
 $C_L = C_o (= 35 \text{ wt\% Ni})$

At  $T_D = 1190^\circ\text{C}$ :  
Only Solid ( $\alpha$ )  
 $C_\alpha = C_o (= 35 \text{ wt\% Ni})$

At  $T_B = 1250^\circ\text{C}$ :  
Both  $\alpha$  and  $L$   
 $C_L = C_{\text{liquidus}} (= 32 \text{ wt\% Ni here})$   
 $C_\alpha = C_{\text{solidus}} (= 43 \text{ wt\% Ni here})$



## Phase Diagrams: weight fractions of phases

- Rule 3: If we know  $T$  and  $C_0$ , then we know the amount of each phase (in wt%).

- Examples:

$C_0 = 35 \text{ wt\% Ni}$

At  $T_A$ : Only Liquid (L)

$$W_L = 100 \text{ wt\%}, W_\alpha = 0$$

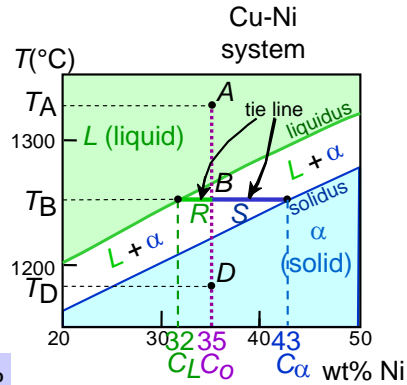
At  $T_D$ : Only Solid ( $\alpha$ )

$$W_L = 0, W_\alpha = 100 \text{ wt\%}$$

At  $T_B$ : Both  $\alpha$  and L

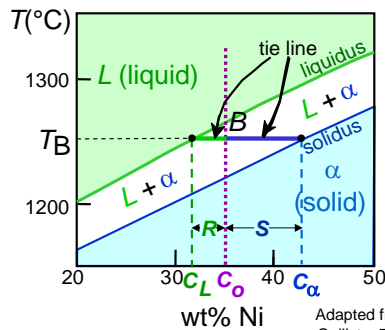
$$W_L = \frac{S}{R+S} = \frac{43-35}{43-32} = 73 \text{ wt\%}$$

$$W_\alpha = \frac{R}{R+S} = 27 \text{ wt\%}$$



## The Lever Rule

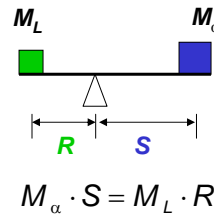
- Tie line – connects the phases in equilibrium with each other: i.e., essentially an iso“therm”



Adapted from Fig. 9.3(b), Callister 7e.

How much of each phase?

Think of it as a lever (teeter-totter)



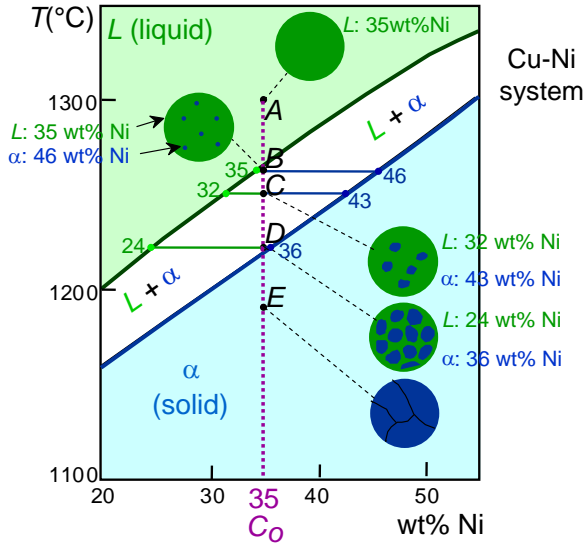
$$M_\alpha \cdot S = M_L \cdot R$$

$$W_L = \frac{M_L}{M_L + M_\alpha} = \frac{S}{R+S} = \frac{C_\alpha - C_0}{C_\alpha - C_L}$$

$$W_\alpha = \frac{R}{R+S} = \frac{C_0 - C_L}{C_\alpha - C_L}$$

## Ex: Cooling in a Cu-Ni Binary

- Phase diagram: Cu-Ni system.
- System is: **binary**  
i.e., 2 components: Cu and Ni.
- isomorphous**  
i.e., complete solubility of one component in another;  $\alpha$  phase field extends from 0 to 100 wt% Ni.
- Consider  $C_0 = 35 \text{ wt\%Ni}$ .



## Frustration during Crystallization

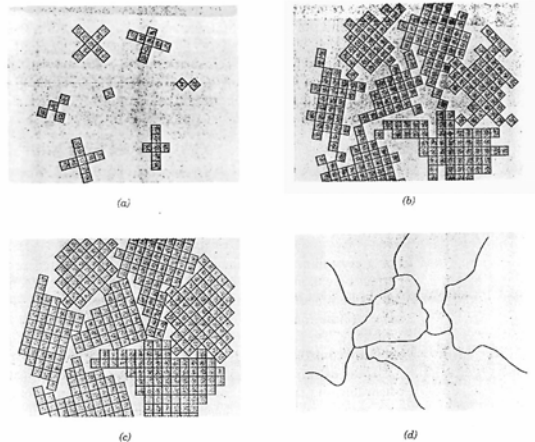
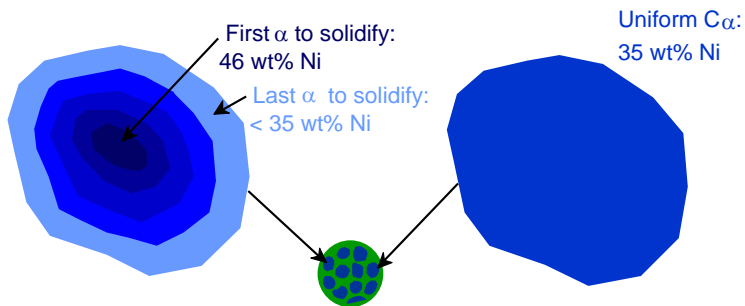


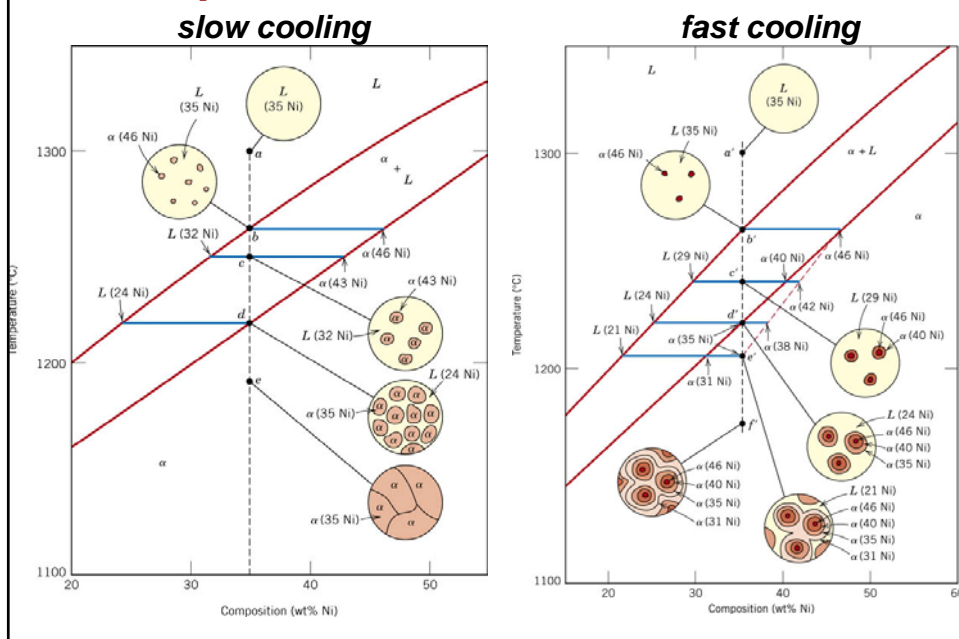
FIGURE 3.16 Schematic diagrams of the various stages in the solidification of a polycrystalline material; the square grids depict unit cells. (a) Small crystallite nuclei. (b) Growth of the crystallites; the obstruction of some grains that are adjacent to one another is also shown. (c) Upon completion of solidification, grains having irregular shapes have formed. (d) The grain structure as it would appear under the microscope; dark lines are the grain boundaries. (Adapted from W. Rosenhain, *An Introduction to the Study of Physical Metallurgy*, 2nd edition, Constable & Company Ltd., London, 1915.)

## Compositional Non-Equilibrium Phases

- $C_{\alpha}$  changes as we solidify.
- Cu-Ni case: First  $\alpha$  to solidify has  $C_{\alpha} = 46 \text{ wt\% Ni}$ .  
Last  $\alpha$  to solidify has  $C_{\alpha} = 35 \text{ wt\% Ni}$ .
- Fast rate of cooling: Cored structure
- Slow rate of cooling: Equilibrium structure



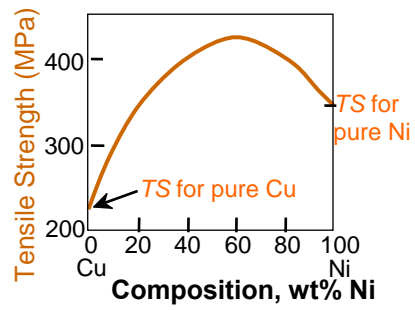
## Equilibrium vs. Cored Phases



## Mechanical Properties: Cu-Ni System

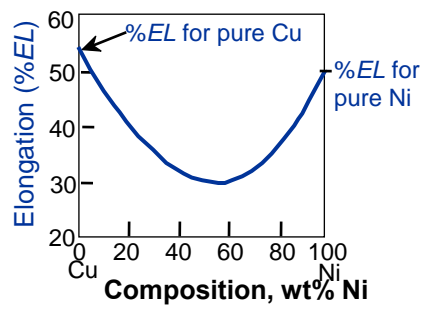
- Effect of solid solution strengthening on:

Tensile strength (TS)



Peak as a function of  $C_0$

Ductility (%EL,%AR)



Min. as a function of  $C_0$

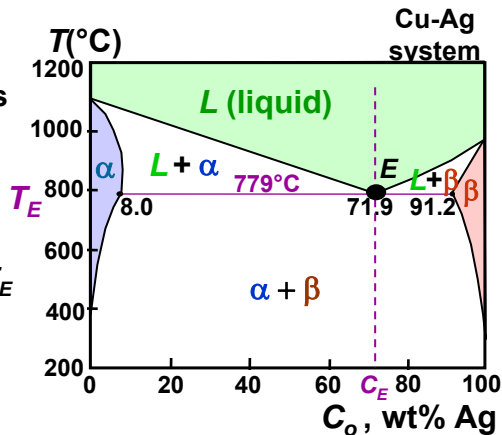
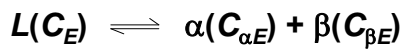
## Binary-Eutectic Systems

2 components

has a special composition with a min. melting T.

Ex.: Cu-Ag system

- 3 single phase regions ( $L, \alpha, \beta$ )
- Limited solubility:
  - $\alpha$ : mostly Cu
  - $\beta$ : mostly Ag
- $T_E$ : No liquid below  $T_E$
- $C_E$ : Min. melting  $T_E$  composition
- Eutectic transition



## Gibbs Phase Rule

$$F = C + N - P$$

F = degrees of freedom necessary to specify the system

(# of ext. variables, e.g., T, P, Comp.)

P = # of phases

C = # of components

N = # of non-compositional variables

At Eutectic

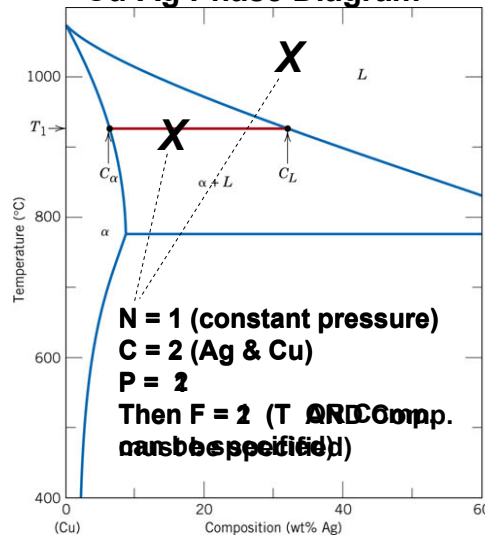
N = 1 (constant pressure)

C = 2 (Ag & Cu)

P = 3

Then F = 0 (no variables)

Cu-Ag Phase Diagram



N = 1 (constant pressure)

C = 2 (Ag & Cu)

P = 2

Then F = 2 (T and Comp. can be specified)

at eutectic

N = 1 (constant pressure)

C = 2 (Ag & Cu)

P = 3

Then F = 0 (no variables)

## Pb-Sn Eutectic System (1)

For a 40 wt% Sn-60 wt% Pb alloy at 150°C, find...

- the phases present:  $\alpha + \beta$

- compositions of phases:

$$C_0 = 40 \text{ wt\% Sn}$$

$$C_\alpha = 11 \text{ wt\% Sn}$$

$$C_\beta = 99 \text{ wt\% Sn}$$

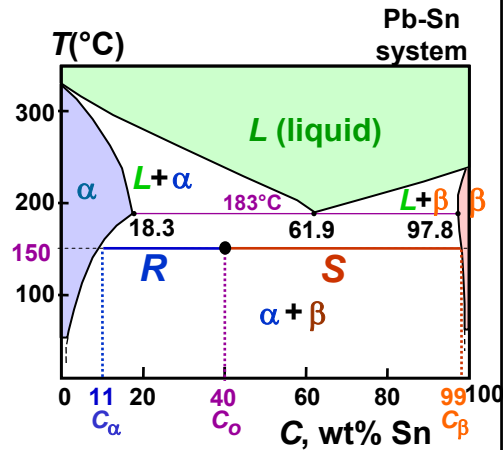
- the relative amount of each phase:

$$W_\alpha = \frac{S}{R+S} = \frac{C_\beta - C_0}{C_\beta - C_\alpha}$$

$$= \frac{99 - 40}{99 - 11} = \frac{59}{88} = 67 \text{ wt\%}$$

$$W_\beta = \frac{R}{R+S} = \frac{C_0 - C_\alpha}{C_\beta - C_\alpha}$$

$$= \frac{40 - 11}{99 - 11} = \frac{29}{88} = 33 \text{ wt\%}$$



## Pb-Sn Eutectic System (2)

For a 40 wt% Sn-60 wt% Pb alloy at 200°C, find...

- the phases present:  $\alpha + L$

- compositions of phases:

$$C_0 = 40 \text{ wt\% Sn}$$

$$C_\alpha = 17 \text{ wt\% Sn}$$

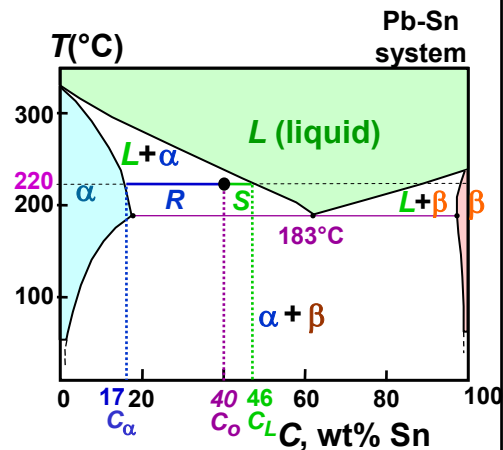
$$C_L = 46 \text{ wt\% Sn}$$

- the relative amount of each phase:

$$W_\alpha = \frac{C_L - C_0}{C_L - C_\alpha} = \frac{46 - 40}{46 - 17}$$

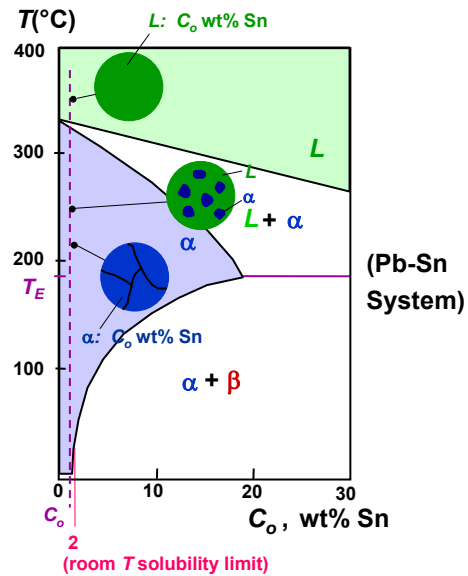
$$= \frac{6}{29} = 21 \text{ wt\%}$$

$$W_L = \frac{C_0 - C_\alpha}{C_L - C_\alpha} = \frac{40 - 17}{46 - 17} = \frac{23}{29} = 79 \text{ wt\%}$$



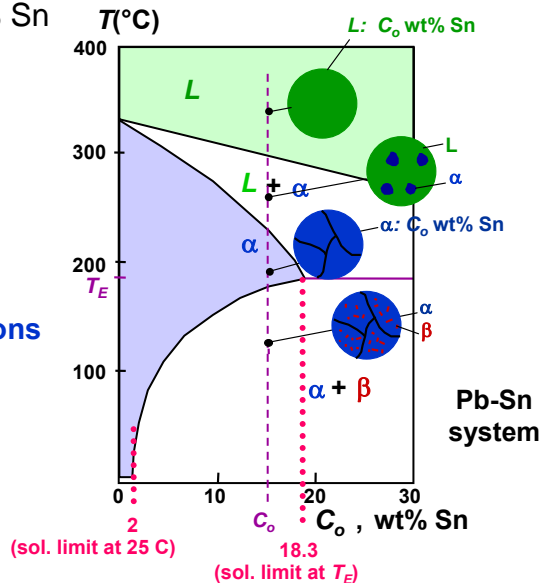
## Microstructures in Eutectic Systems: I

- $C_o < 2 \text{ wt\% Sn}$
- Result:  
polycrystal of  $\alpha$  grains only  
i.e., only one solid phase.

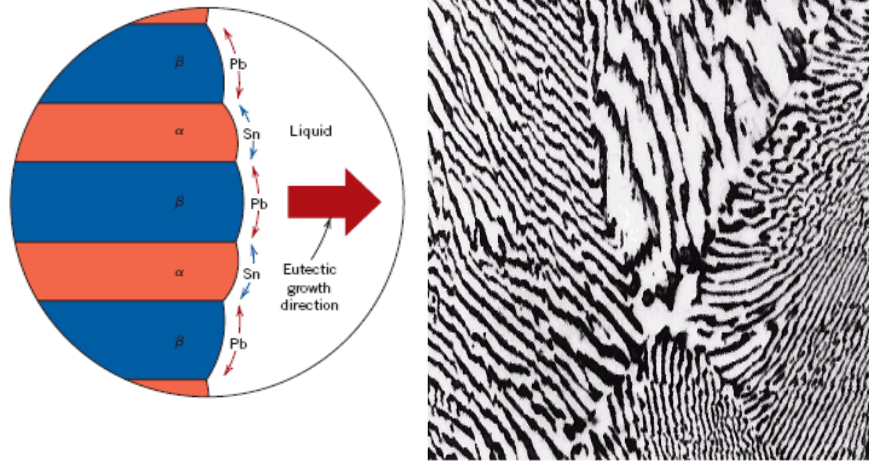


## Microstructures in Eutectic Systems: II

- $2 \text{ wt\% Sn} < C_o < 18.3 \text{ wt\% Sn}$
- Result:
  - Initially liquid +  $\alpha$
  - then  $\alpha$  alone
  - finally two phases  
 $\alpha$  polycrystal  
fine  $\beta$ -phase inclusions

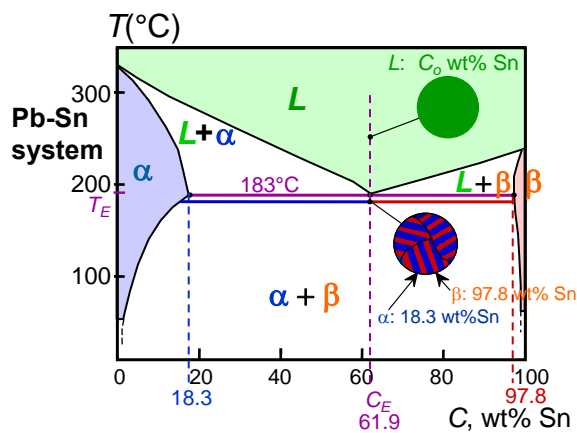


## Lamellar Eutectic Structure



## Microstructures in Eutectic Systems: III

- $C_0 = C_E$
- **Result:** Eutectic microstructure (lamellar structure) alternating layers (lamellae) of  $\alpha$  and  $\beta$  crystals.



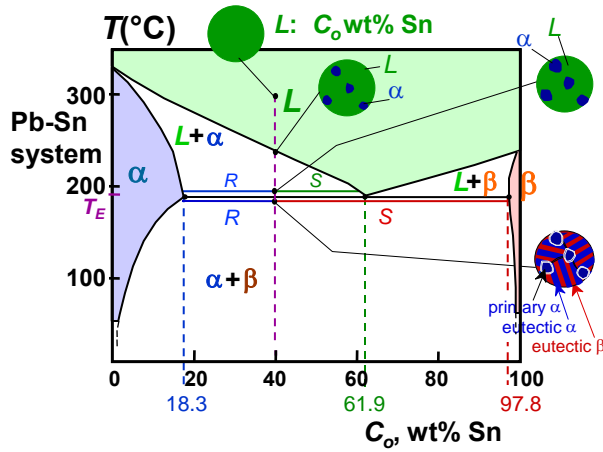
Micrograph of Pb-Sn eutectic microstructure



160  $\mu\text{m}$

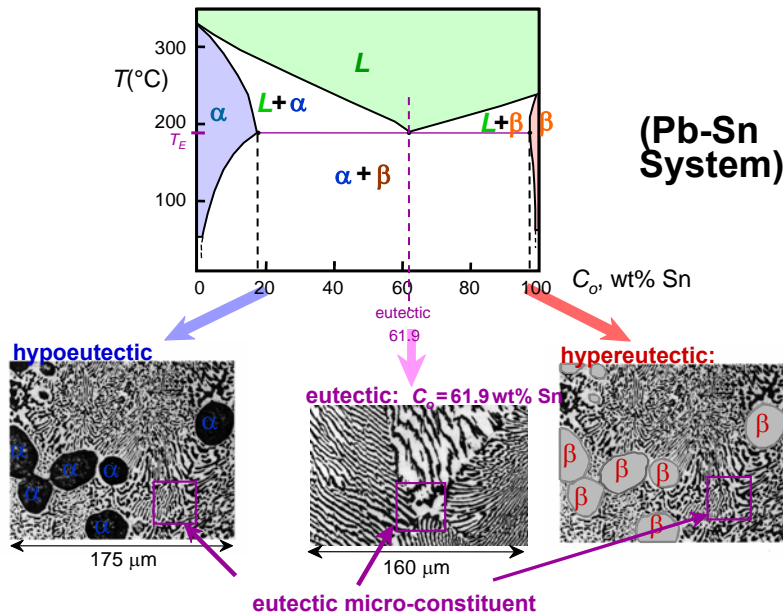
# Microstructures in Eutectic Systems: IV

- 18.3 wt% Sn < C<sub>0</sub> < 61.9 wt% Sn
- **Result:** α crystals and a eutectic microstructure

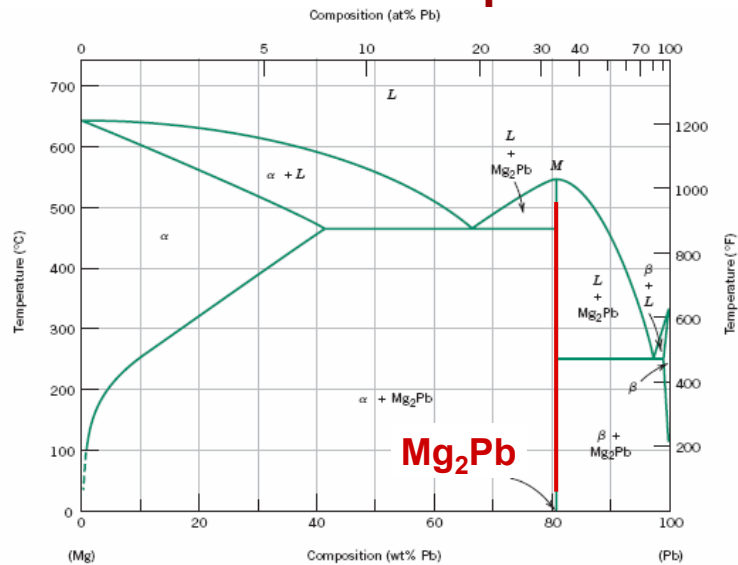


- Just above T<sub>E</sub>:
  - C<sub>α</sub> = 18.3 wt% Sn
  - C<sub>L</sub> = 61.9 wt% Sn
  - $W_α = \frac{S}{R+S} = 50 \text{ wt\%}$
  - $W_L = (1 - W_α) = 50 \text{ wt\%}$
- Just below T<sub>E</sub>:
  - C<sub>α</sub> = 18.3 wt% Sn
  - C<sub>β</sub> = 97.8 wt% Sn
  - $W_α = \frac{S}{R+S} = 73 \text{ wt\%}$
  - W<sub>β</sub> = 27 wt%

# Hypoeutectic & Hypereutectic



## Intermetallic Compounds



**Note: intermetallic compound forms a line - not an area - because stoichiometry (i.e. composition) is exact.**

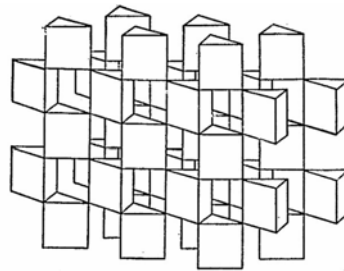
## Fe-C Phase Equilibria

**Ferrite:** BCC  $\alpha$ -Fe Relatively soft and ductile; magnetic at RT.  
Max C solubility 0.022%

**Austenite:** FCC  $\gamma$ -Fe Ductile only at elevated temperatures;  
nonmagnetic at high temperatures.  
Max C solubility 2.1%

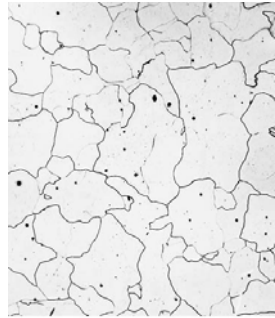
**Cementite:** Fe<sub>3</sub>C a Compound,  
not an alloy. 6.69% C.

**Martensite:** a grain structure not a phase.  
Crystal structure is formed by  
displacive transformation  
(i.e., unit cell distortion),  
not by much slower diffusion.

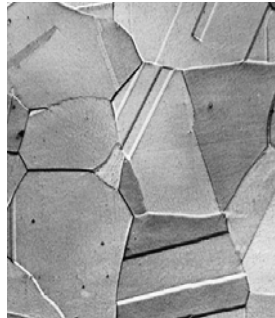


The structure of cementite, Fe<sub>3</sub>C, as a packing of CFe<sub>6</sub> trigonal prisms

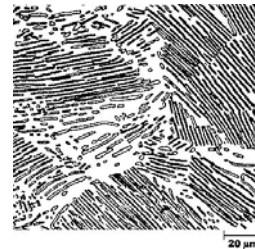
## Fe-C Phase Equilibria



**Ferrite**



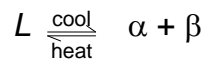
**Austenite**



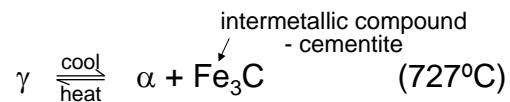
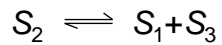
**Pearlite**  
(cementite+ austenite)

## Eutectoid & Peritectic

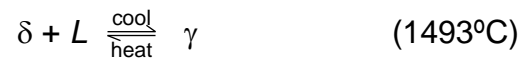
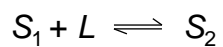
- **Eutectic:** liquid in equilibrium with two solids



- **Eutectoid:** solid phase in equilibrium with 2 solid Phases



- **Peritectic:** liquid + solid 1 in equilibrium with solid 2



## Eutectoid

**Eutectoid Transformation:** A solid-solution conversion to a mixture of solids.

e.g., Fe-C: austenite phase can undergo a eutectoid transformation to produce ferrite and cementite (iron carbide), often in lamellar structures such as pearlite and bainite.

This eutectoid point is at about 0.6% carbon; alloys of nearly this composition are called **high-carbon steel**, while those which do not undergo eutectoid transformation are termed **mild steel**.

The process analogous to glass formation in this system is the **martensitic** transformation.

## Peritectic

**Peritectic Transformation:** when a liquid and solid phase of fixed proportions react at a fixed temperature to yield a single solid phase.

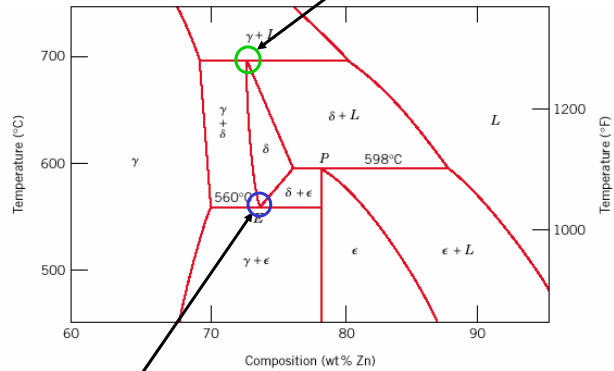
Since the solid product forms at the interface between the two reactants, it can form a diffusion barrier and generally causes such reactions to proceed much more slowly than eutectic or eutectoid transformations.

Because of this, when a peritectic composition solidifies it does not show the lamellar structure (which is typical of eutectic freezing).

## Eutectoid & Peritectic

### Cu-Zn Phase diagram

Peritectic transition  $\gamma + L \rightleftharpoons \delta$



Eutectoid transition  $\delta \rightleftharpoons \gamma + \epsilon$

## Fe-C Phase Equilibria

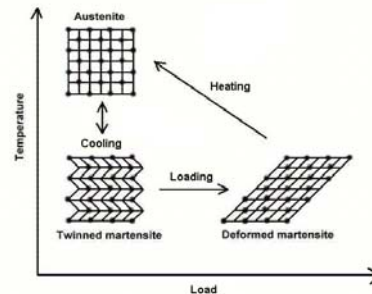
**Martensite:** a grain structure not truly a phase.

Crystal structures formed by displacive transformation (i.e., unit cell distortion), not by much slower diffusive transformations. Often form lenticular (lens-shaped) crystal grains (which appear needle-shaped in x-section).

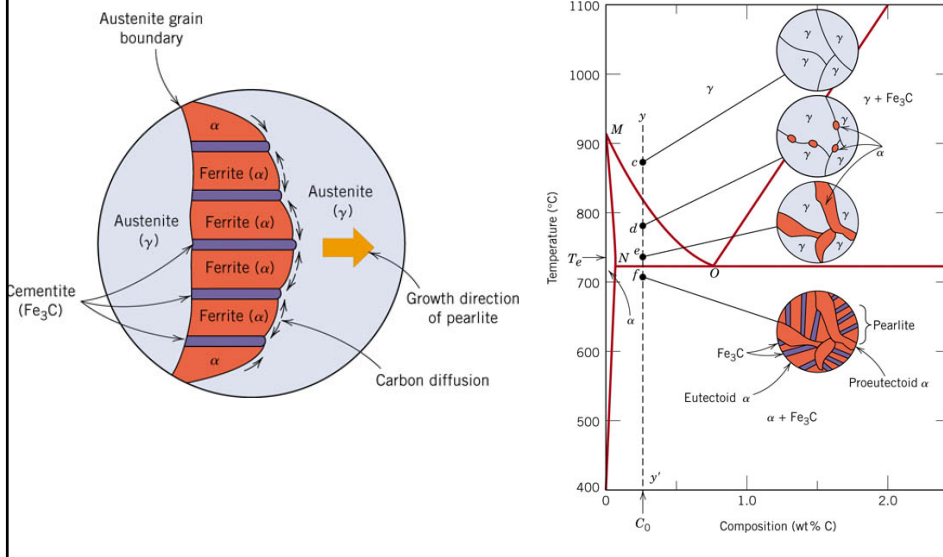
Martensite is specifically a form of ferrite supersaturated with C => very hard steels (springs and piano wire).

Martensite is formed by rapid cooling of austenite which traps carbon atoms that do not have time to diffuse out of the crystal structure.

Martensite “phases” show memory effects.  
[http://www.lassp.cornell.edu/sethna/Tweed/What\\_Are\\_Martensites.html](http://www.lassp.cornell.edu/sethna/Tweed/What_Are_Martensites.html)



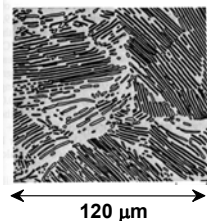
## Diffusional Frustration during Crystallization



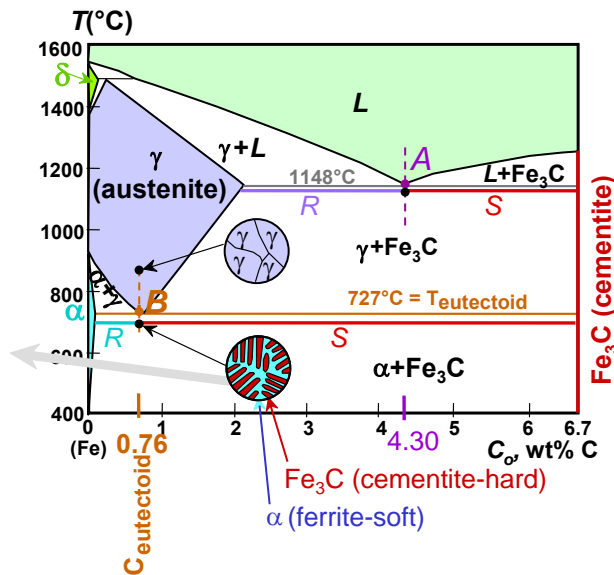
## Iron-Carbon (Fe-C) Phase Diagram

**Eutectic (A):**  
 $L \Rightarrow \gamma + \text{Fe}_3\text{C}$

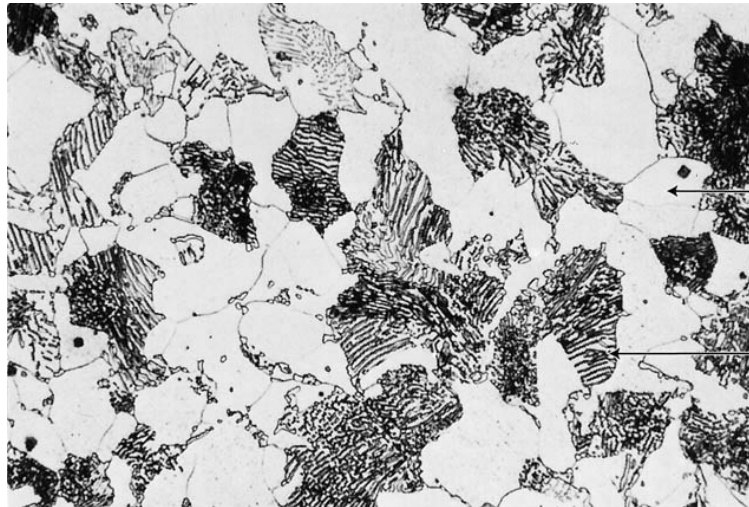
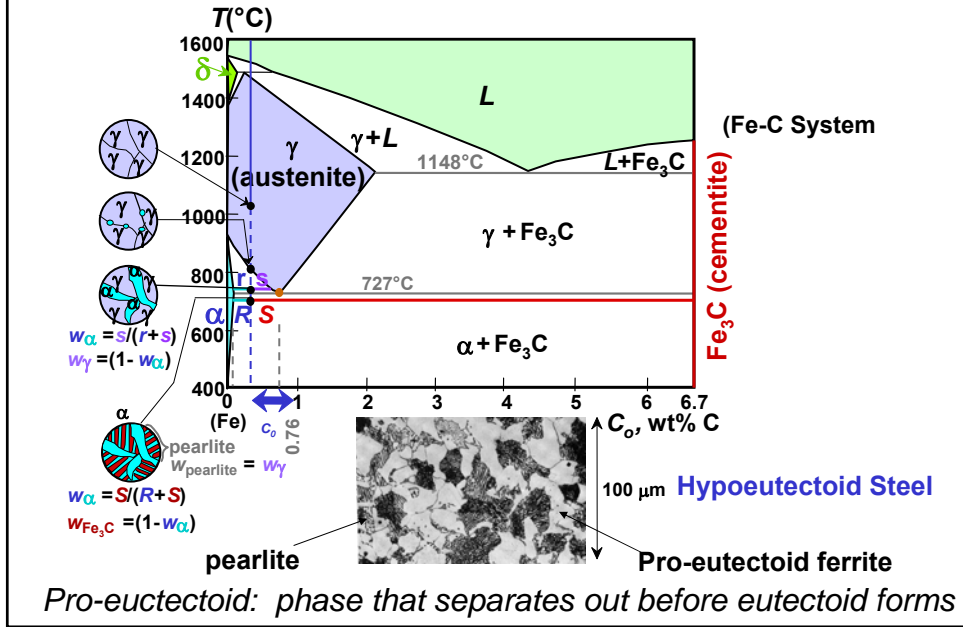
**Eutectoid (B):**  
 $\gamma \Rightarrow \alpha + \text{Fe}_3\text{C}$



**Result: Pearlite = alternating layers of  $\alpha$  and  $\text{Fe}_3\text{C}$  phases**

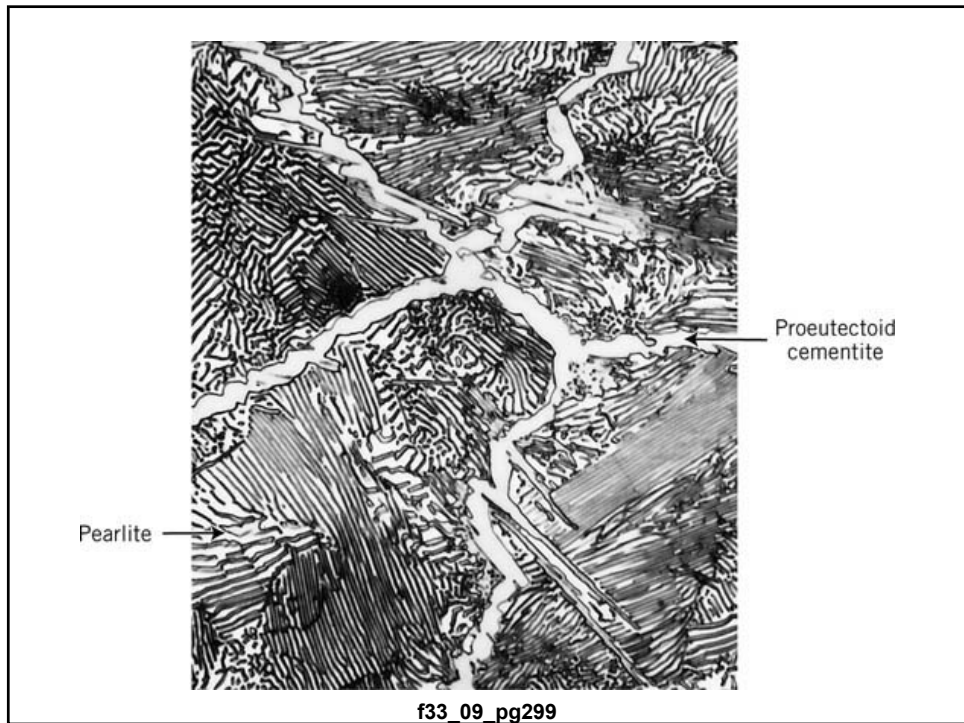
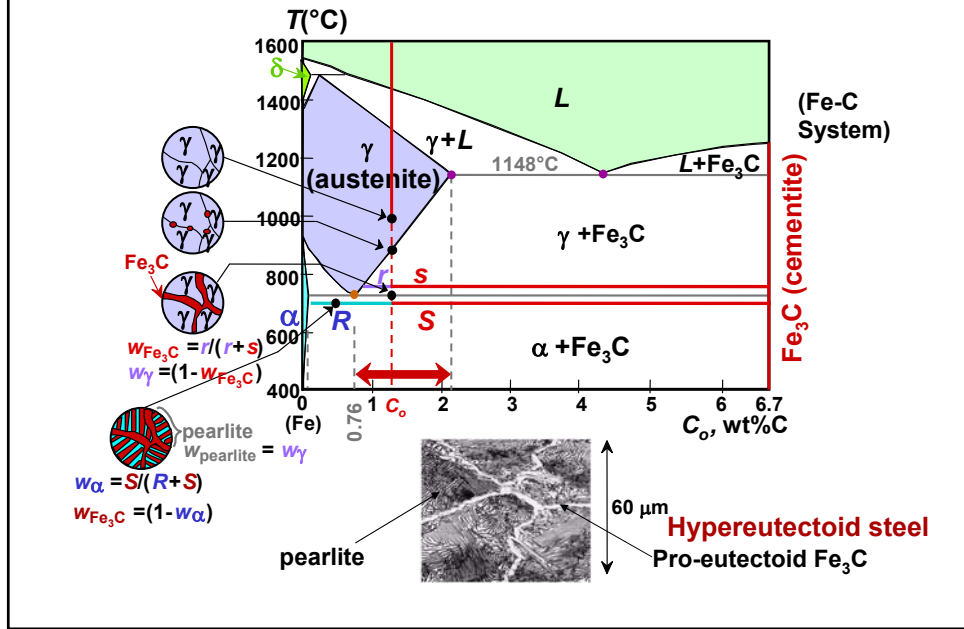


# Hypoeutectoid Steel



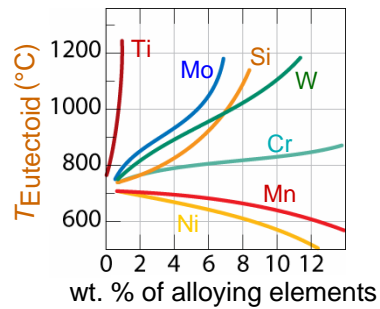
f30\_09\_pg296

# Hypereutectoid Steel

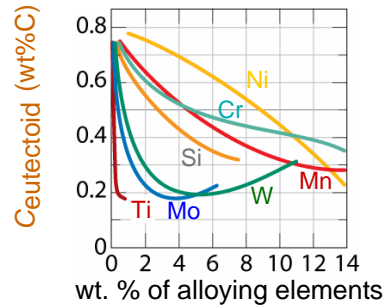


## Alloying Steel with More Elements

- $T_{\text{eutectoid}}$  changes:

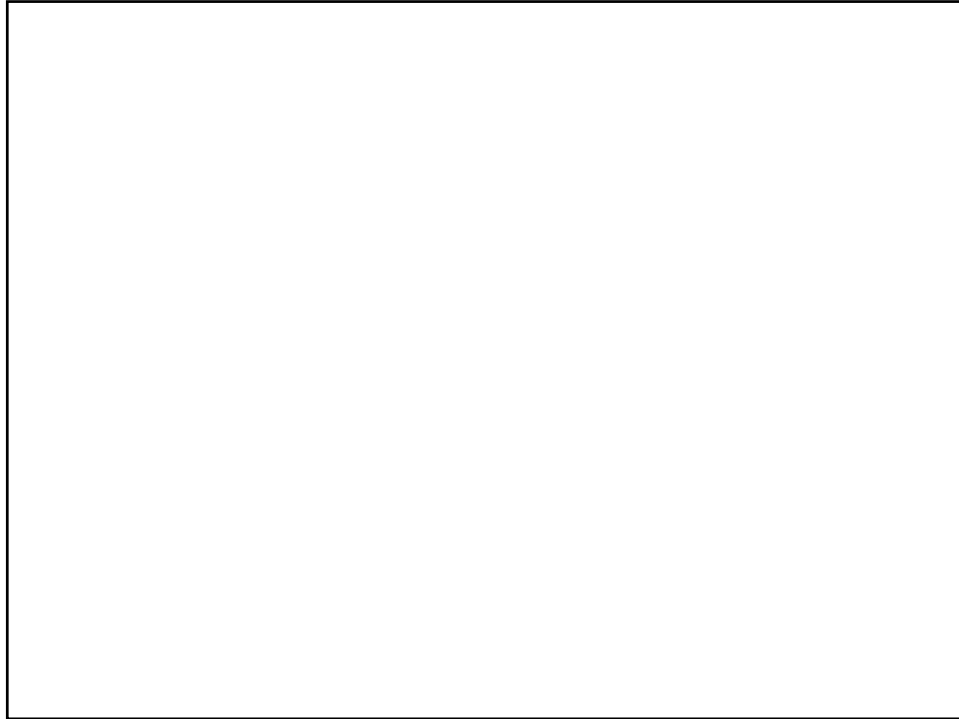


- $C_{\text{eutectoid}}$  changes:



## Summary

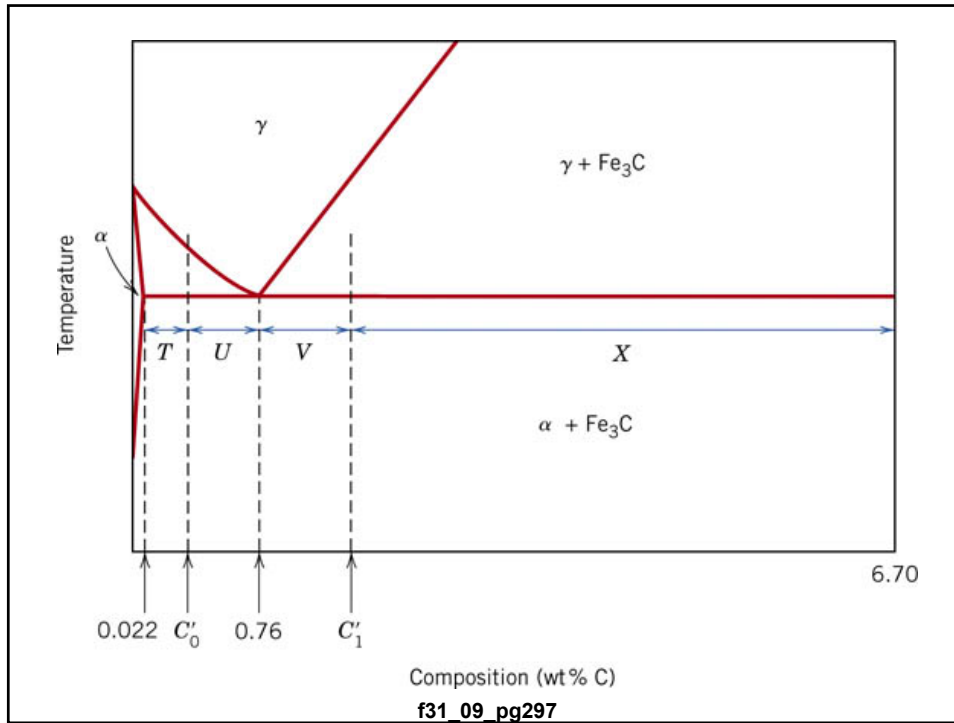
- **Phase diagrams** are useful tools to determine for a given  $T$  and composition of the system
  - the number and types of phases,
  - the wt% of each phase,
  - and the **composition** of each phase
- Alloying to produce a solid solution usually
  - increases the tensile strength ( $TS$ )
  - decreases the ductility.
- Binary **eutectics** and binary **eutectoids** allow for a range of microstructures.



### **Example: Phase Equilibria**

For a 99.6 wt% Fe-0.40 wt% C at a temperature just below the eutectoid, determine the following

- a) composition of  $\text{Fe}_3\text{C}$  and ferrite ( $\alpha$ )
- b) the amount of carbide (cementite) in grams that forms per 100 g of steel
- c) the amount of pearlite and pro-eutectoid ferrite ( $\alpha$ )



## Phase Equilibria

**Solution:** a) composition of  $\text{Fe}_3\text{C}$  and ferrite ( $\alpha$ )

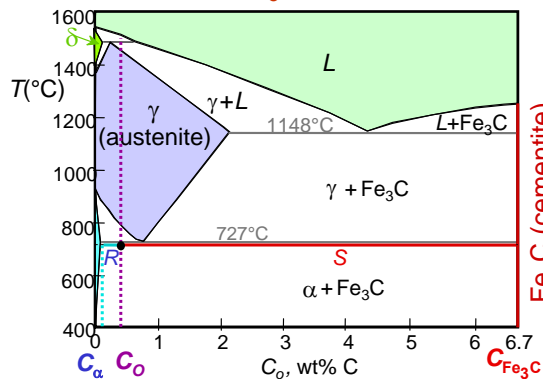
b) the amount of carbide (cementite) in grams that forms per 100 g of steel

$C_0 = 0.40 \text{ wt\% C}$   
 $C_\alpha = 0.022 \text{ wt\% C}$   
 $C_{\text{Fe}_3\text{C}} = 6.70 \text{ wt\% C}$

$$\frac{\text{Fe}_3\text{C}}{\text{Fe}_3\text{C} + \alpha} = \frac{C_0 - C_\alpha}{C_{\text{Fe}_3\text{C}} - C_\alpha} \times 100$$

$$= \frac{0.4 - 0.022}{6.7 - 0.022} \times 100 = 5.7\text{g}$$

$\text{Fe}_3\text{C} = 5.7 \text{ g}$   
 $\alpha = 94.3 \text{ g}$



## Phase Equilibria

- c. the amount of pearlite and proeutectoid ferrite ( $\alpha$ )  
 note: amount of pearlite = amount of  $\gamma$  just above  $T_E$

$C_o = 0.40 \text{ wt\% C}$   
 $C_\alpha = 0.022 \text{ wt\% C}$   
 $C_{\text{pearlite}} = C_\gamma = 0.76 \text{ wt\% C}$

$$\frac{\gamma}{\gamma + \alpha} = \frac{C_o - C_\alpha}{C_\gamma - C_\alpha} \times 100 = 51.2 \text{ g}$$

pearlite = 51.2 g  
 proeutectoid  $\alpha$  = 48.8 g

